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This implies that there are infinitely many human beings.

But, history of mankind is finite, so there are only finitely many human beings.

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What's wrong?

- May be the statement “*everybody has a mother*” is incorrect. Thus f is not a function (*some inputs do not give any output*).
- Or H is not a set; *there may be something between human and non-human*.